

Statistics

Lecture 24



Feb 19-8:47 AM

Testing one population Proportion: (SG 24)

$$\begin{array}{lcl}
 1) & \left. \begin{array}{l} H_0: P = P_0 \\ H_1: P \neq P_0 \end{array} \right\} & \left. \begin{array}{l} H_0: P \leq P_0 \\ H_1: P > P_0 \end{array} \right\} & \left. \begin{array}{l} H_0: P \geq P_0 \\ H_1: P < P_0 \end{array} \right\} \\
 & \text{TTT} & \text{RTT} & \text{LTT}
 \end{array}$$

Always identify the claim & type of testing

2) Find all Critical values

Drawing, labeling, Shading, Full TI Command needed. use invNorm.

3) Find Computed Test statistics CTS and P-value P.

use TI Command 1-PropZTest

4) We use the testing chart to determine the validity of H_0 & H_1 .

H_0 valid $\Leftrightarrow H_1$ invalid

H_0 invalid $\Leftrightarrow H_1$ valid

5) Draw final conclusion about the claim.

Reject the claim
when claim is invalid

OR **Fail to Reject the claim**
when claim is valid.

May 14-1:51 PM

College **claims** that **10% of all** students smoke.

$P = .1$
 H_0

I surveyed 250 students and 30 of them were smokers.
 $n = 250$ $x = 30$

use $\alpha = .1$ to test the claim.

$H_0: P = .1$ claim
 $H_1: P \neq .1$ TTT

CV Z TTT $\alpha = .1$

CTS Z
P-Value P

1-Prop ZTest
 $P_0: .1$ H_0
 $x = 30$
 $n = 250$
Prop $\neq P_0$
Calculate

$Z = \text{invNorm}(.95, 0, 1)$

CTS $Z = 1.054$
P-Value $P = .292$

CTS is in NCR.
 H_0 Valid \rightarrow Valid claim
 H_1 invalid FTR the claim

$P\text{-value} > \alpha$
 $.292 > .1$
 H_0 Valid, H_1 invalid
Valid claim \rightarrow FTR the claim

May 14-2:02 PM

CNN **claims** that **at most 45% of all** voters are in favor of term limits for politicians.

$P \leq .45$
 H_0

I surveyed 750 voters, and 48% of them were in favor of term limits.
 $n = 750$
 $x = .48(750) = 360$

Test the claim using $\alpha = .02$

$H_0: P \leq .45$ claim
 $H_1: P > .45$ RTT

CV Z RTT $\alpha = .02$

CTS Z
P-Value P

1-Prop ZTest
 $P_0: .45$ H_0
 $x: 360$
 $n: 750$
Prop $> P_0$ H_1
Calculate

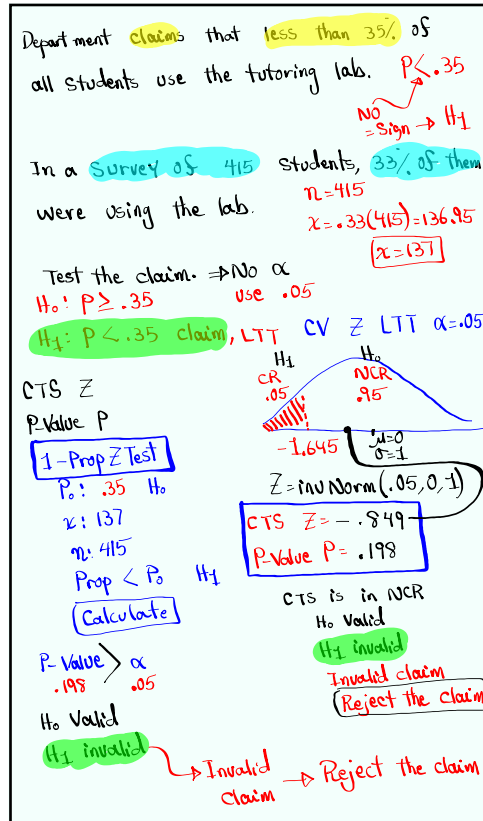
$Z = \text{invNorm}(.98, 0, 1)$

CTS $Z = 1.651$
P-Value $P = .049$

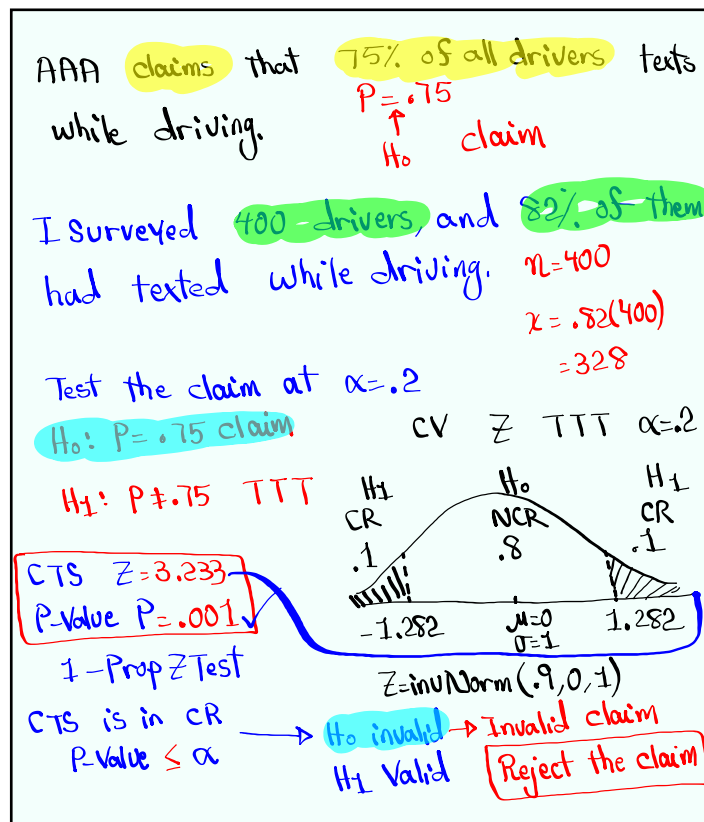
CTS is in NCR.
 H_0 Valid \rightarrow Valid claim
 H_1 invalid FTR the claim

$P\text{-value} > \alpha$
 $.049 > .02$
 H_0 Valid
 H_1 invalid. FTR the claim

May 14-2:19 PM



May 14-2:35 PM



May 14-2:52 PM

College claims that more than 70% of all students are in favor of in-person classes.

$P > .7$
 \nwarrow No sign $\rightarrow H_1$
 $=$ sign

A survey of 570 students, 68% of them were fan of in-person classes.

$n = 570$
 $x = .68(570)$
 $= 387.6$
 $\boxed{x = 388}$

Test the claim. $\alpha \rightarrow .05$

$H_0: P \leq .7$

$H_1: P > .7$ claim, RTT

CTS $Z = -1.005$

P-value $P = .843$

1-Prop Z Test

$P_0: .7$
 $x = 388$
 $n = 570$
 $\text{Prop} > P_0$
 $\boxed{\text{Calculate}}$

CV Z RTT $\alpha = .05$

H_0 NCR H_1 CR

$\mu = 0$ $\sigma = 1$ 1.645

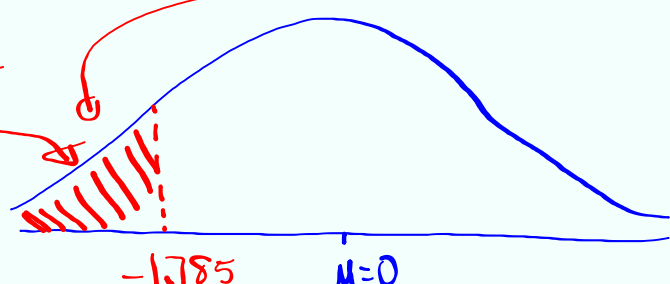
$Z = \text{inUNorm}(.95, 0, 1)$

CTS is in NCR
 $P\text{-value} > \alpha$
 H_0 Valid
 H_1 invalid \Rightarrow Invalid claim
Reject the claim

May 14-3:09 PM

Given CTS $Z = -1.785$, LTT

find p-value.



$\rightarrow \text{normalcdf}(-E99, -1.785, 0, 1) = \boxed{.037}$

If it was TTT $\Rightarrow 2(.037) = \boxed{.074}$

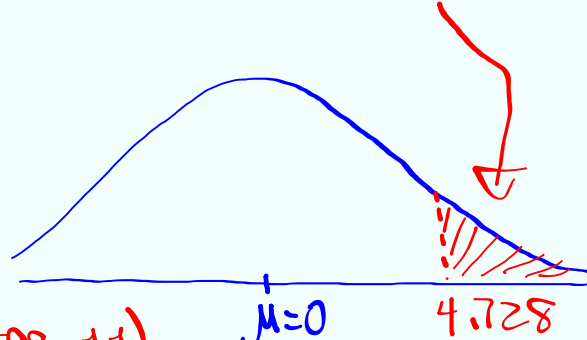
May 14-3:23 PM

Given CTS $t = 4.728$, $df = 11$, RTT

Find P-Value

$$t_{cdf}(4.728, E99, 11) = 3.1 \times 10^{-4}$$

$\mu = 0$
 σ unknown
 $df = 11$



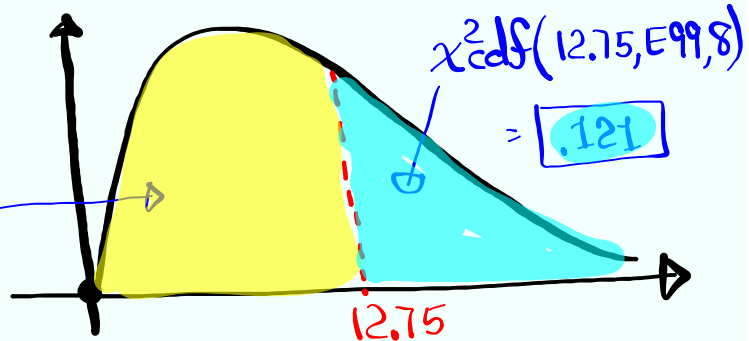
If it was TTT $\Rightarrow 2(3.1 \times 10^{-4})$
 6.2×10^{-4}

May 14-3:28 PM

Given CTS $\chi^2 = 12.75$, $df = 8$, TTT.

Find P-Value

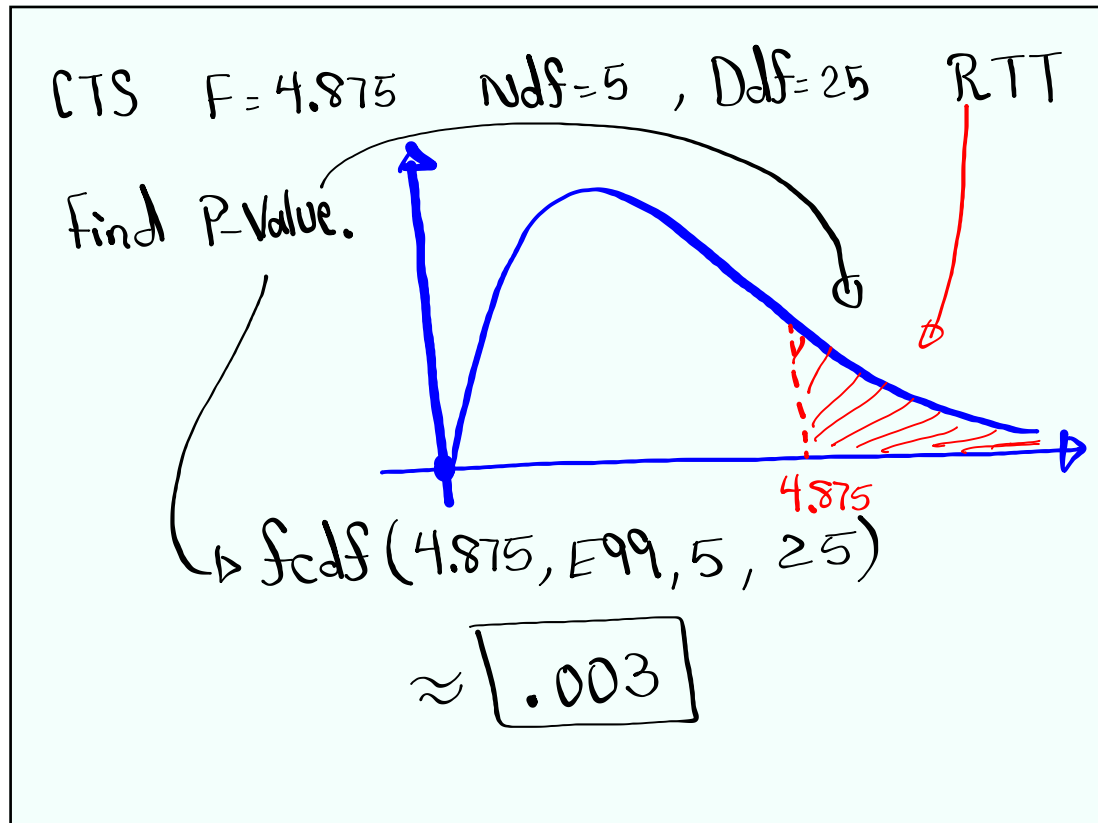
$$\chi^2_{cdf}(0, 12.75, 8) = .879$$



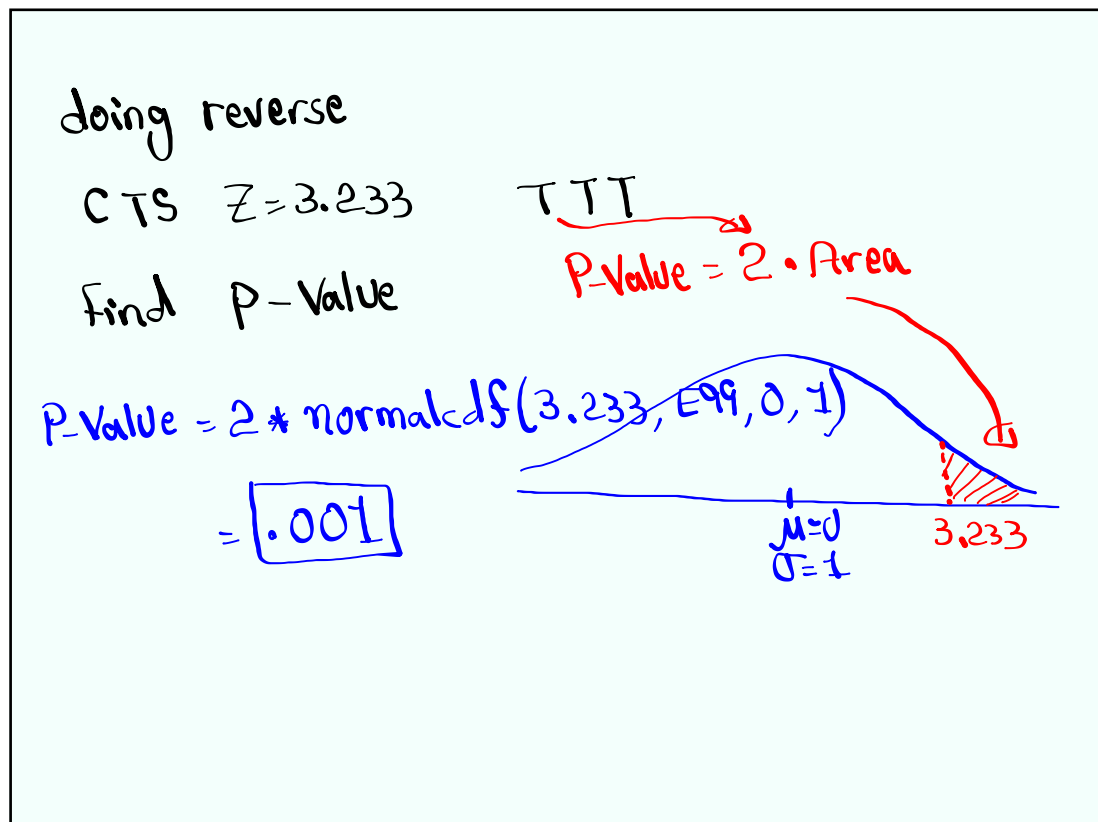
P-Value = 2 • Smaller area

$$= 2 (.121) = .242$$

May 14-3:32 PM



May 14-3:37 PM



May 14-3:06 PM